

Solution

ADMISSION TEST

Class 10 - Admission Test

1.

(c) 4851

Explanation:

Let the radius of the spherical ball be r

and side of the cube is a

According to the question,

$$\text{No. of cubes} = \frac{\text{Volume of spherical ball}}{\text{Volume of a cube}}$$

$$= \frac{\frac{4}{3}\pi r^3}{a^3}$$

$$\text{No. of cubes} = \frac{4 \times 22 \times 21 \times 21 \times 21}{3 \times 7 \times 2 \times 2 \times 2 \times (1)^3} = 4851$$

2.

(d) 0

Explanation:

The abscissa of any point on y-axis is always zero. This means that this point hasn't covered any distance on x-axis.

3.

(b) $\frac{4}{7}$

Explanation:

$$P(E) + P(\text{not } E) = 1$$

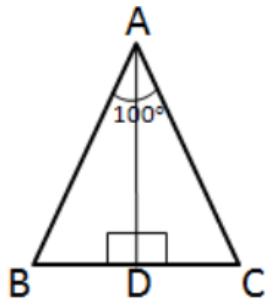
$$\text{The probability of happening of an event} = \frac{3}{7}$$

$$\text{The probability of not happening of this event} = 1 - \frac{3}{7} = \frac{4}{7}$$

4.

(b) 40°

Explanation:



$AD \perp BC$ and AD bisects $\angle A$

$$\Rightarrow \angle BAD = \angle CAD = 50^\circ$$

In Right $\triangle ADB$

$$\angle BAD = 50^\circ, \angle ADB = 90^\circ$$

Also sum of all interior angles = 180°

$$\Rightarrow \angle BAD + \angle ADB + \angle B = 180^\circ$$

$$\Rightarrow \angle B = 180^\circ - 50^\circ - 90^\circ$$

$$\Rightarrow \angle B = 40^\circ$$

5.

(c) $\frac{3}{10}$

Explanation:

No. of favourable outcomes = 12

Total outcomes = 40

Required Probability = $12/40 = 3/10$

6.

(c) $\frac{3}{10}$

Explanation:

The smallest rational number by which $\frac{1}{3}$ should be multiplied so that its decimal expansion terminates after one place of decimal, is $\frac{3}{10}$

Since, $\frac{1}{3} \times \frac{3}{10} = \frac{1}{10} = 0.1$

Since, among them $\frac{3}{10}$ is the only number which when multiplied, then its decimal expansion terminates after one place of decimal.

7.

(c) 216

Explanation:

Let the radius of the smaller sphere be r cm

and the radius of the bigger sphere is R cm.

Then according to question,

$$\begin{aligned}\text{No. of spherical balls} &= \frac{\text{Volume of a solid sphere}}{\text{Volume of a spherical ball}} = \frac{\frac{4}{3}\pi R^3}{\frac{4}{3}\pi r^3} \\ &= \frac{R^3}{r^3} \\ &= \frac{6^3}{1^3} = 216\end{aligned}$$

8.

(c) $\frac{1}{5}$

Explanation:

$$(125)^{-1/3}$$

$$=(5^3)^{-1/3}$$

$$=5^{-1}$$

$$\frac{1}{5}$$

9.

(b) there are infinitely many rational numbers

Explanation:

Between two rational number, there infinitely many rational number.

e.g., $\frac{3}{5}$ and $\frac{4}{5}$ are two rational number, then $\frac{31}{50}, \frac{32}{50}, \frac{33}{50}, \frac{34}{50}, \frac{35}{50}, \dots$ are infinite rational numbers between them.

10. (a) $\frac{5}{7}$

Explanation:

The probability that a boy will get married to his girlfriend, $P(E) = \frac{2}{7}$

The probability that he will not get married to his girlfriend, $P(\text{not } E) = 1 - P(E) = 1 - \frac{2}{7} = \frac{5}{7}$

11.

(c) $\sqrt{\frac{3}{8} \times \frac{5}{8}}$

Explanation:

An irrational number between $\frac{3}{8}$ and $\frac{5}{8}$ is $\sqrt{\frac{3}{8} \times \frac{5}{8}}$

12. (a) $6 : \pi$

Explanation:

Let side of cube be a

Here, side of cube = diameter of sphere

so, radius of sphere = $\frac{a}{2}$

The volume of cube : volume of sphere

$$a^3 : \frac{4}{3} \pi r^3$$

$$a^3 : \frac{4}{3} \pi \left(\frac{a}{2}\right)^3$$

$$3 \times 8 \times a^3 : 4\pi a^3$$

$$6 : \pi$$

13. (a) $\frac{1}{4}$

Explanation:

$$\left(3x + \frac{1}{2}\right) \left(3x - \frac{1}{2}\right) = 9x^2 - p$$

$$\Rightarrow (3x)^2 - \left(\frac{1}{2}\right)^2 = 9x^2 - p$$

$$\Rightarrow 9x^2 - \frac{1}{4} = 9x^2 - p$$

$$\Rightarrow p = \frac{1}{4}$$

14.

(b) quadrant I and II

Explanation:

Since, sign of point in 1st quadrant is (+, +),

And in second quadrant it is (—, +)

So, Ordinate of a point is +ve only in 1st and 2nd quadrant

15. (a) 4: 25

Explanation:

Let r_1, r_2 be the radii of the two cones respectively, then Required ratio,

$$\begin{aligned} & \frac{\frac{1}{3} \pi r_1^2 h}{\frac{1}{3} \pi r_2^2 h} \\ &= \frac{r_1^2}{r_2^2} \\ &= \left(\frac{r_1}{r_2}\right)^2 \\ &= \left(\frac{2}{5}\right)^2 = \frac{4}{25} \\ &= 4 : 25 \end{aligned}$$

16.

(c) x-axis

Explanation:

Since the ordinates of given points are 0. Therefore, points lie on x-axis.

17.

(d) 322

Explanation:

On cubing we get

$$\left(x + \frac{1}{x}\right)^3 = x^3 + \left(\frac{1}{x^3}\right) + 3 \cdot x \cdot \frac{1}{x} \left(x + \frac{1}{x}\right)$$

$$\Rightarrow 27 = x^3 + \left(\frac{1}{x^3}\right) + 3 \cdot 3$$

$$\Rightarrow x^3 + \left(\frac{1}{x^3}\right) = 27 - 9$$

$$\Rightarrow x^3 + \left(\frac{1}{x^3}\right) = 18$$

$$\text{Now, } \left(x^3 + \frac{1}{x^3}\right)^2 = x^6 + \left(\frac{1}{x^6}\right) + 2 \cdot x^3 \cdot \frac{1}{x^3}$$

$$\Rightarrow 18^2 = x^6 + \left(\frac{1}{x^6}\right) + 2$$

$$x^6 + \left(\frac{1}{x^6}\right) = 324 - 2 = 322$$

18.

(d) $3\sqrt{3}$

Explanation:

$$2\sqrt{3} + \sqrt{3} = \sqrt{3}(2 + 1) = 3\sqrt{3}$$

19.

(b) -10

Explanation:

Since $x = 2$ is a zero. Put $x = 2$ in the equation

$$(2)^2 + 3(2) + k = 0$$

$$4 + 6 + k = 0$$

$$k = -10$$

20.

(a) $\frac{29}{40}$

Explanation:

Total number of bulbs in the lot = 80

Number of bulbs with life time of more than 500 hours =

$$23 + 25 + 10 = 58$$

Let E be the event that the chosen bulb's life time is more than 500 hours.

$$\therefore \text{Required probability} = P(E) = \frac{58}{80} = \frac{29}{40}$$

21.

(a) 16 years

Explanation:

Manick's present age = 12 years, Rahul's present age = 4 years.

Let Manick be twice as old as Rahul after x years from now.

$$\text{Then, } 12 + x = 2(4 + x) \Leftrightarrow 12 + x = 8 + 2x \Leftrightarrow x = 4.$$

Hence, Manick's required age = $12 + x = 16$ years.

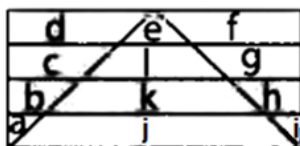
22.

(d) 12 triangles, 10 rectangles

Explanation:

Triangle formed are: a, ab, abc, adcd, e, el, elk, elkj, i, ih, ihg, ihgf, i.e. 12 in number

Rectangles formed are: def, clg, bkh, aji, defclg, clgbkh, bkhaji, defclgbkh, clgbkhaji and a big rectangle, i.e. 10 in number.



23.

(d) D and C

Explanation:

D and C

24.

(b) $P \varnothing Q \# R - S + T$

Explanation:

' $P \varnothing Q \# R - S + T$ ' means P is wife of Q who is father of R and R is sister of S, who is brother of T. Clearly, S is male and P is the mother of R, S and T.

25.

(d) NHOHTSFQ

Explanation:

Logic: Every alphabet at odd place move forward by 1 and at even place move backward by 1.

TERMITE = UDSLJSF

So, MINISTER = NHOHTSFQ

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